

# デュアルTHzコム分光法

徳島大学ポストLEDフォトリニクス研究所 (pLED)  
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分子研セミナー@2022/6/30

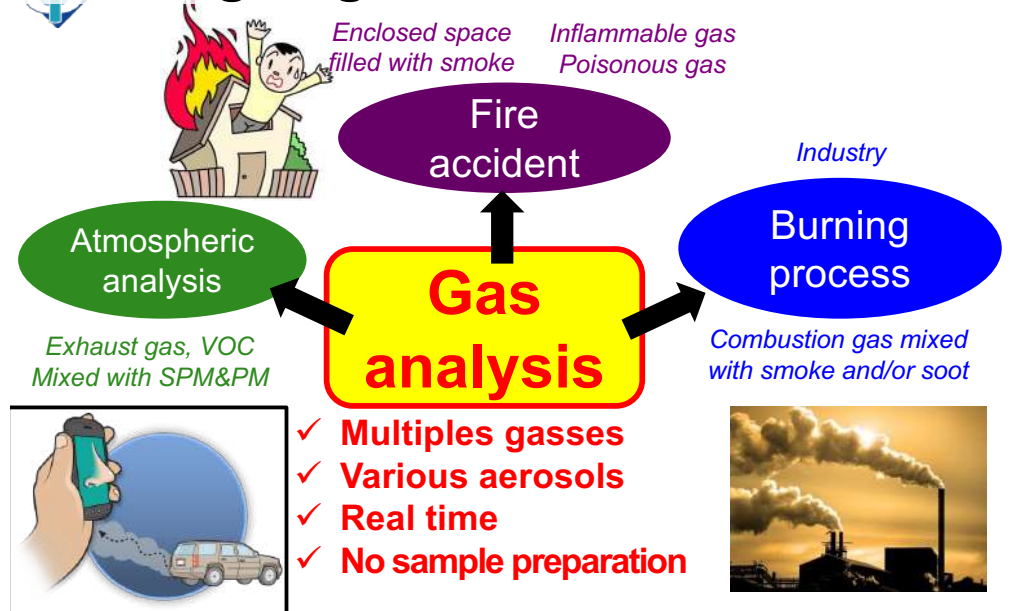
# Outline

1. Introduction
2. Dual THz comb spectroscopy (THz-DCS)
3. Gapless THz-DCS
4. Adaptive sampling THz-DCS using a single, free-running fiber laser
5. Summary

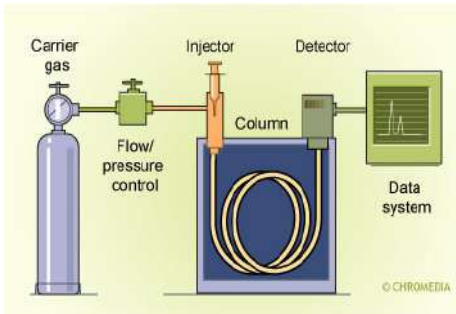
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# Sensing of gas mixed with aerosols

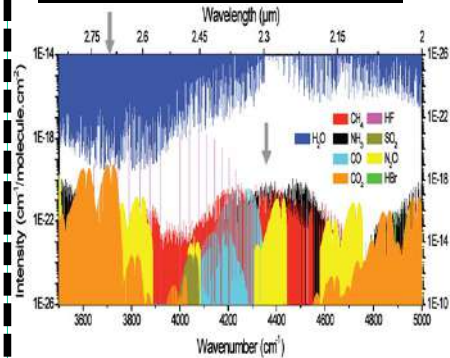


## Gas chromatography

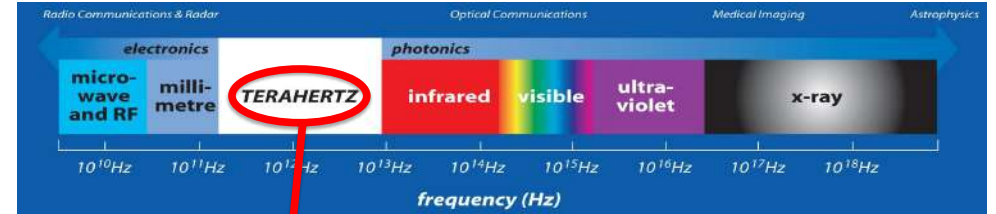


**High sensitivity, high resolution**  
**Limited multiple analysis**  
**Sample preparation**  
**Long analysis time**

## Infrared spectroscopy



**Real time**  
**Multiple gas analysis**  
**No sample preparation**  
**Sensitive to scattering**



- both characteristics of optical and electric waves
- coherent beam
- low invasion
- **less scattering**
- good penetration
- **THz spectral fingerprints**

## (1) Rotational transitions of polar molecules

- ✓ Rich spectral fingerprints with high sensitivity
- ✓ High molecular selectivity based on rotational transition
- ✓ High molecular discrimination at low pressure due to narrow Doppler linewidth (~1MHz)

## (2) Less scattering

- ✓  $\lambda_{\text{THz}} \gg$  particle diameter
- ✓ Possible to analyze gas molecules mixed with aerosols, fog, cloud, smoke, soot, etc

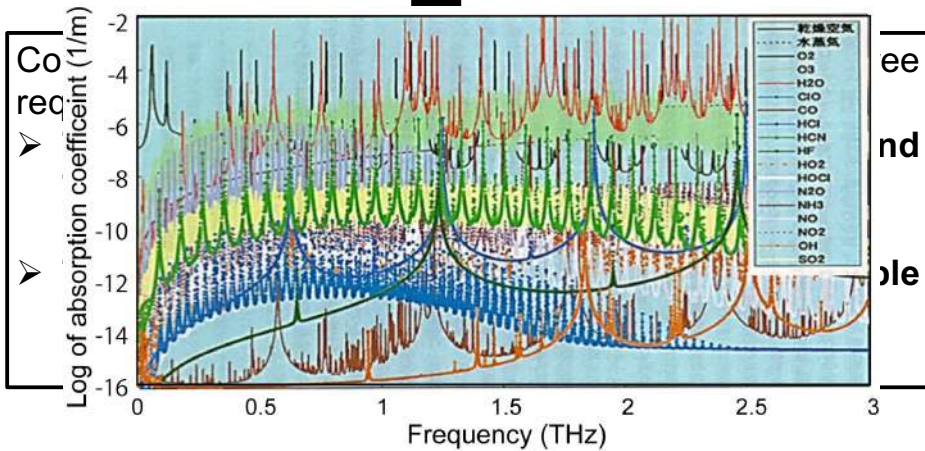
## (1) Rotational transitions of polar molecules

- ✓ Rich spectral fingerprints with high sensitivity
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## (2) Less scattering

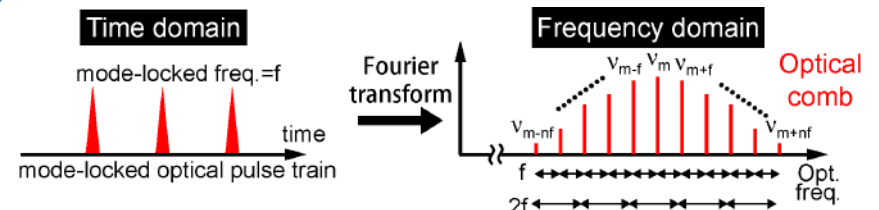
- ✓  $\lambda_{\text{THz}} \gg$  particle diameter
- ✓ Possible to analyze gas molecules mixed with aerosols, fog, cloud, smoke, soot, etc

To discriminate the target gas correctly, high resolution, high accuracy, and broad spectrum are required simultaneously in THz region!

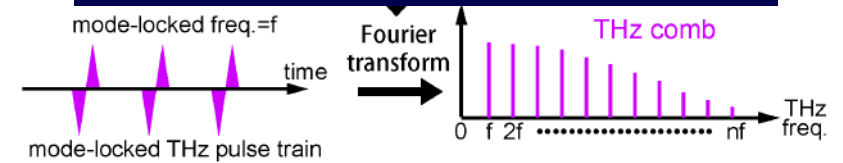


**THz frequency comb**

## Optical comb and THz comb



**Precise frequency marker for broadband THz spectrum**



Simple, broadband selectivity, high spectral purity, and absolute frequency calibration



## Outline

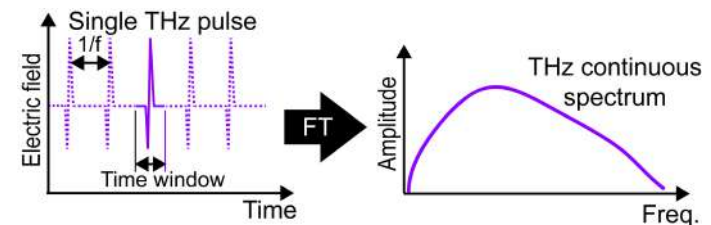


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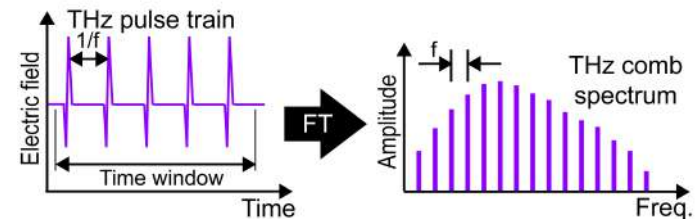
## How measure mode-resolved THz comb spectrum?

Ref) IEEE Trans. THz Sci. Tech. 3, pp. 322-330 (2013).

Traditional THz-TDS equipped with mechanical time-delay scanning



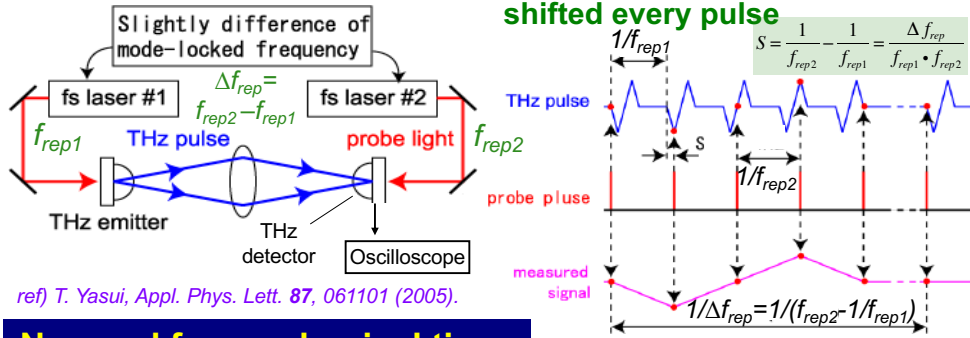
**Time-window-extended THz-TDS**



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# Asynchronous-optical-sampling THz-TDS (ASOPS-THz-TDS)

Overlap timing between THz and probe pulses is automatically shifted every pulse

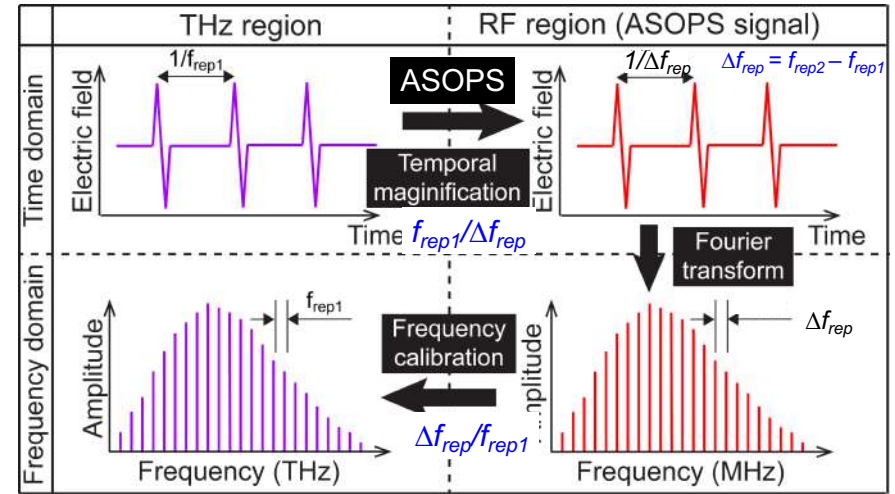


- No need for mechanical time-delay scanning
- No limitation for size of time window

Time scale of ps THz pulse is linearly expanded to μs order

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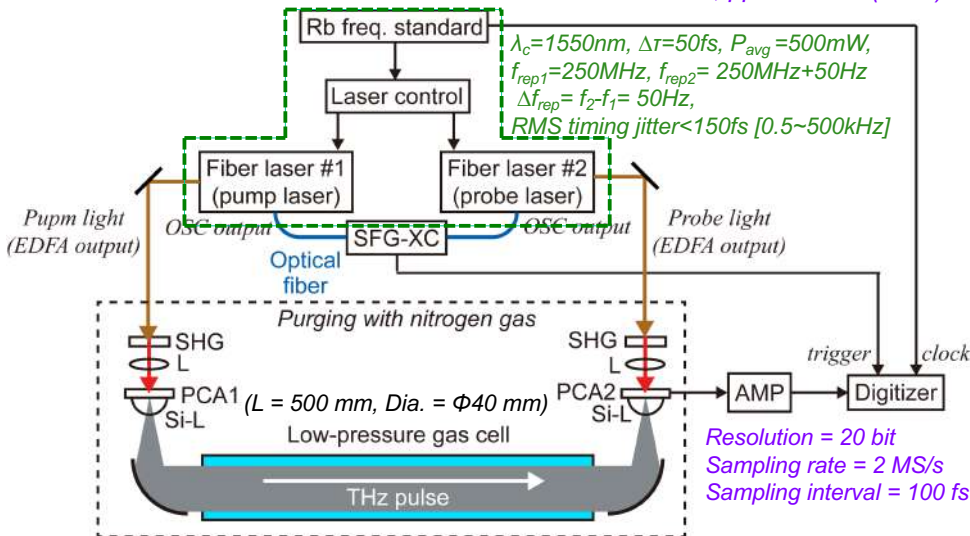
# Signal flowchart in THz-DCS



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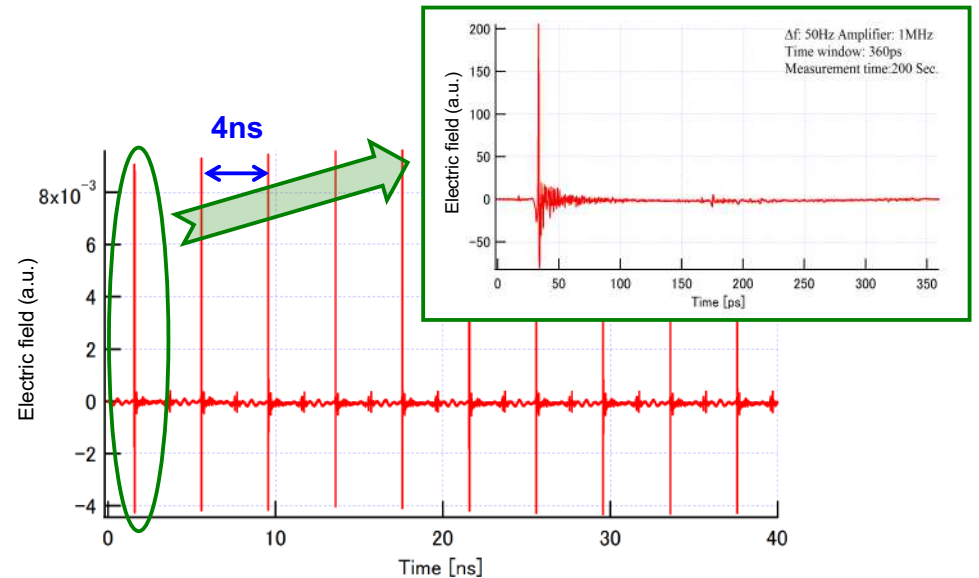
# Experimental setup

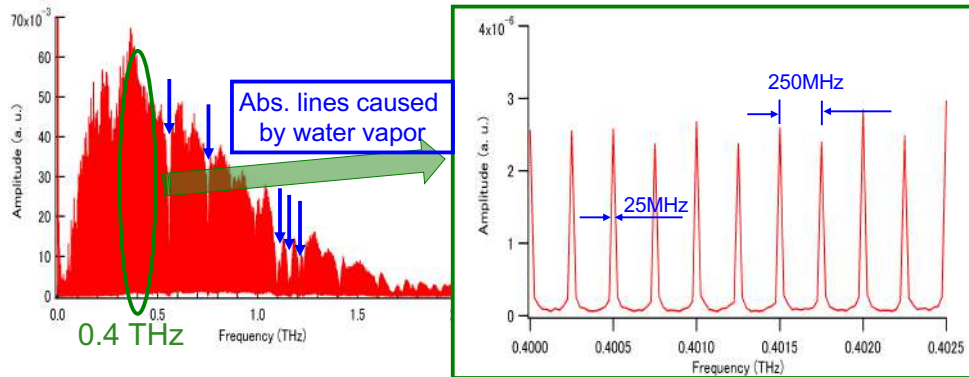
Ref) IEEE Trans. THz Sci. Tech. 3, pp. 322-330 (2013).



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# Temporal waveform of 10 consecutive THz pulses



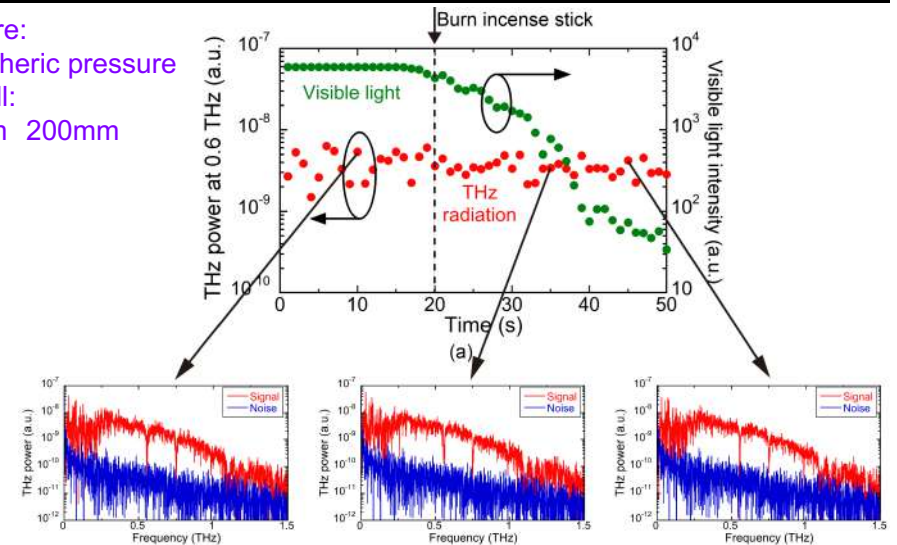


Frequency spacing = 250MHz = mode-locked frequency  
 Mode linewidth = 25 MHz = inverse of time window

# Immunity to smoke scattering

Comparison of power between THz radiation and visible light

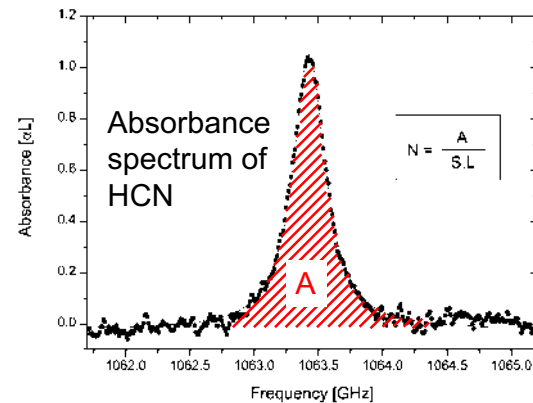
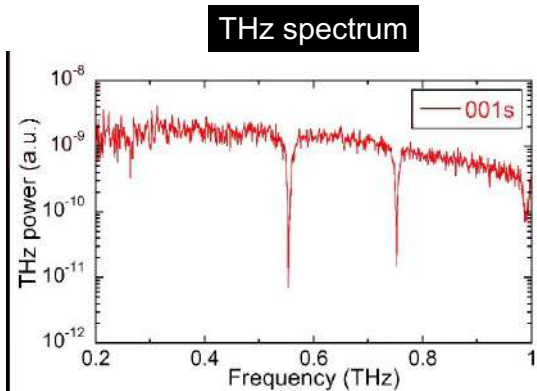
Pressure: atmospheric pressure  
 Gas cell:  $\Phi 50\text{mm}$  200mm length



Measurement rate = 1 Hz

## Experimental procedure

- Pressure: atmospheric pressure  
 Gas cell:  $\Phi 50\text{mm}$  200mm length
- (1) Gas cell was filled with smoke.
  - (2)  $\text{CH}_3\text{CN}$  liquid droplet was put into the cell.
  - (3)  $\text{CH}_3\text{CN}$  liquid was evaporated.
  - (4)  $\text{CH}_3\text{CN}$  gas was diffused.



Curve fitting with Lorentzian function

$$\alpha(\nu)L = \frac{A}{\pi} \frac{\Delta\nu}{(\nu - \nu_0)^2 + \Delta\nu^2}$$



$$N = \frac{A}{SL}$$

$N$ : concentration (molecules/cm<sup>3</sup>)  
 $A$ : line area  
 $S$ : line intensity  
 $L$ : interaction length

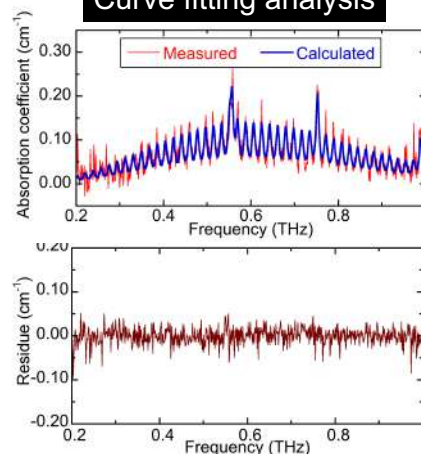
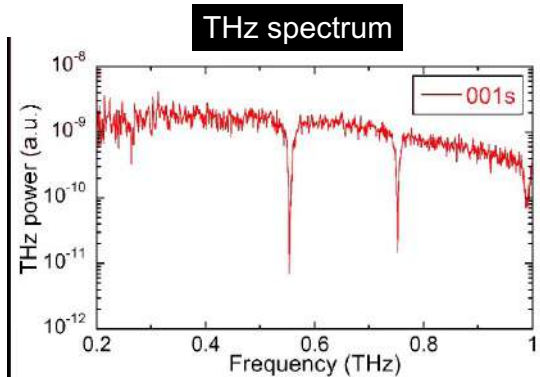
Fitting analysis considering all pressure-broadening absorption lines (> 400 lines)

Ref) F. Hindle, C. R. Phys. **9**, 262–275 (2008).

# Dynamic THz spectroscopy

Measurement rate = 1 Hz

## Curve fitting analysis



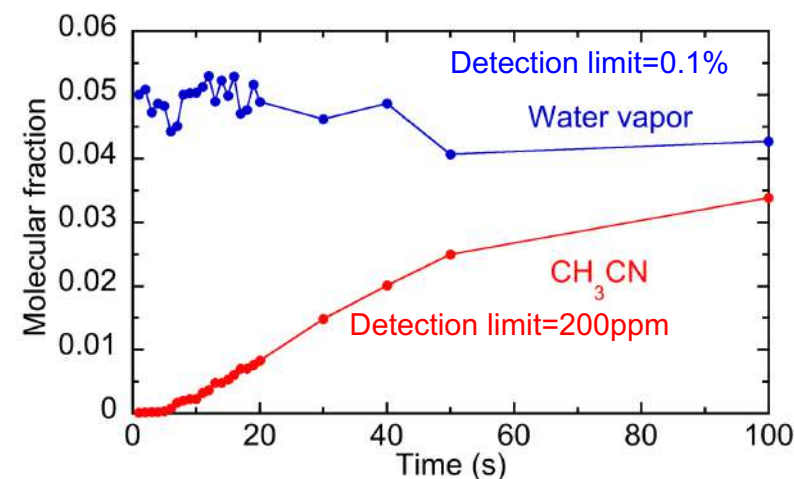
Fitting analysis of all absorption lines of CH<sub>3</sub>CN and H<sub>2</sub>O



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# Temporal change of gas concentration



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# Detection limit of other gasses (measurement rate = 1Hz)

Molecule	Number of absorption lines	Total integrated intensity (nm <sup>2</sup> MHz)	Estimated detection limit
CH <sub>3</sub> CN	900	7.5	200 ppm
CO	7	0.0082	18%
NO <sub>2</sub>	3220	0.045	3%
HCN	9	7.9	200 ppm
HCl	2	0.10	1.5%
SO	135	2.4	600 ppm
SO <sub>2</sub>	2397	2.0	700 ppm



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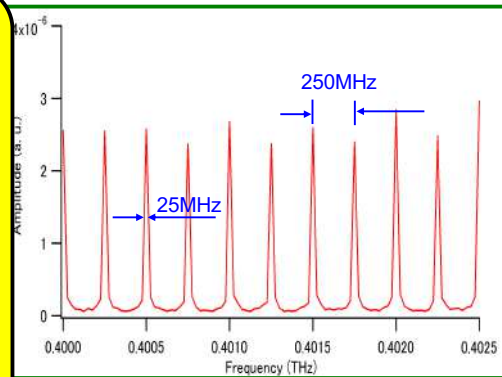
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# Mode-resolved THz comb spectrum

Comb mode can be used as a frequency marker for broadband spectrum

Spectral sampling interval = frequency spacing

Mode linewidth  $\ll$  Frequency spacing



25 MHz = mode-locked frequency  
Mode linewidth = 25 MHz = inverse of time window

# Interleave additional frequency marks into frequency gap

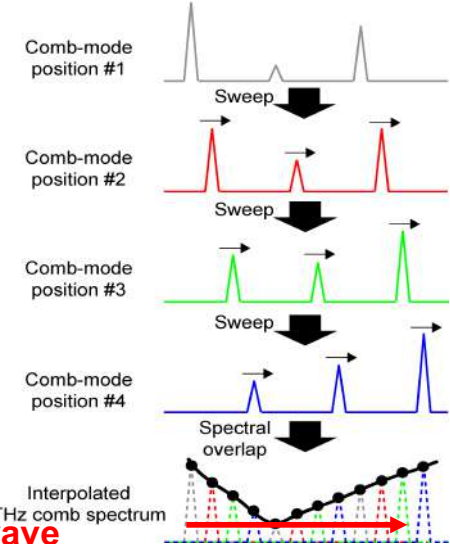
Ref) *Sci. Rep.* 4, 3816 (2014).  
*Optica* 2, 460-467 (2015).

$f_{rep1}, f_{rep2}$ : sweep  
 $\Delta f_{rep}$ : constant

- Incremental sweeping at intervals of linewidth of comb mode
- Overlapping of all spectra

Gap between comb mode can be fully filled!

Equivalent to continuous sweeping of single CW-THz wave



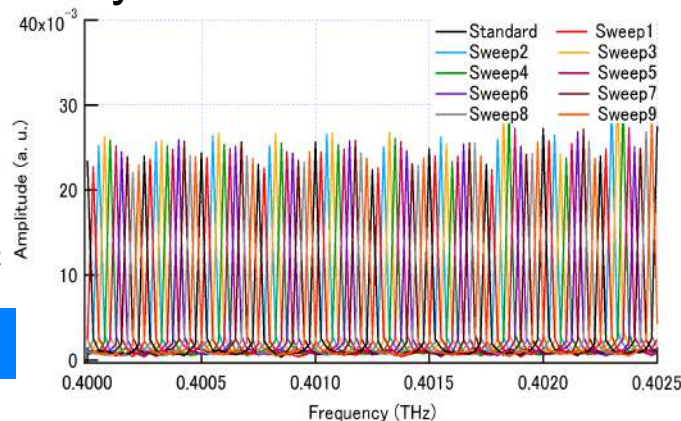
# Sweep of THz comb mode by changing of ML frequency in dual fiber lasers

Before sweeping  
 $f_{rep1} = 250,000,049$  Hz  
 $f_{rep2} = 250,000,099$  Hz  
 $\Delta f_{rep} = 50$  Hz

$f_{rep1} \& f_{rep2}$   
+15,625 Hz

$\Delta f_{rep}$ :  
constant

Incremental sweeping is repeated 10-time

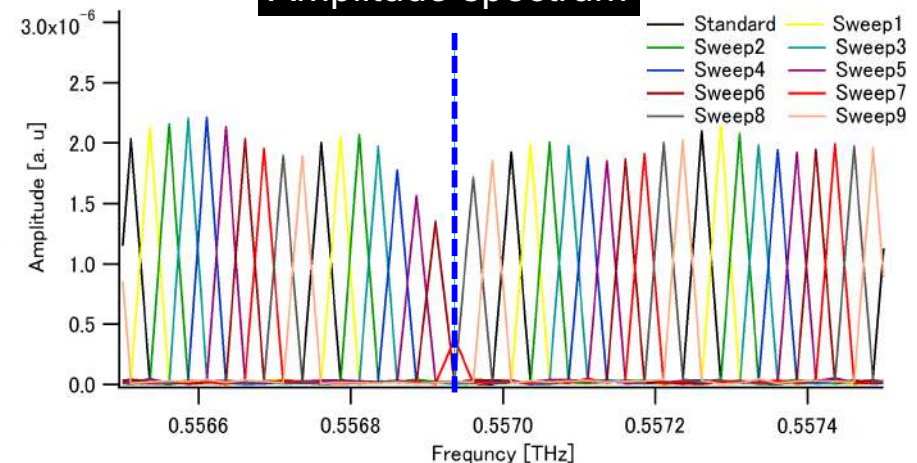


Frequency gaps between comb modes are fully filled!  
Gap-less THz comb was achieved!

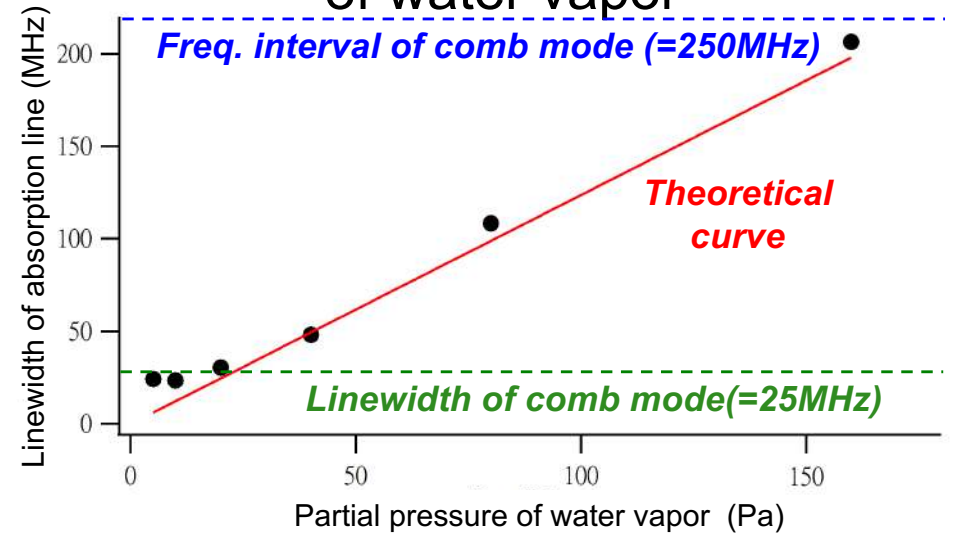
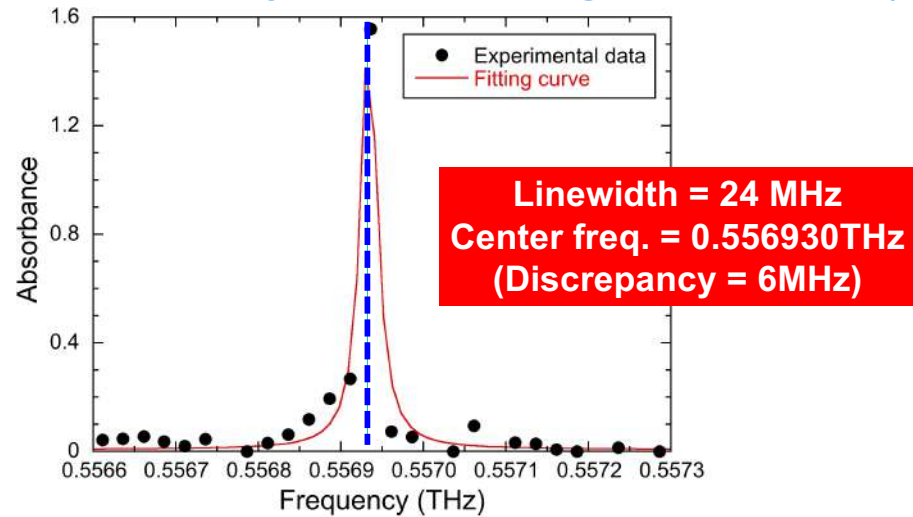
# Spectroscopy of low-pressure water vapor

Rotational transition  $1_{10} \leftarrow 1_{01}$ : 0.5569360 THz @ NASA database  
(Pressure broadening linewidth = 23 MHz @ H<sub>2</sub>O: 10 Pa & N<sub>2</sub>: 320 Pa)

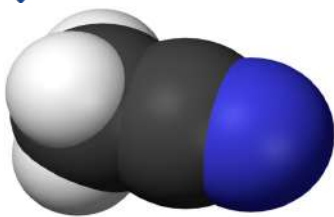
Amplitude spectrum



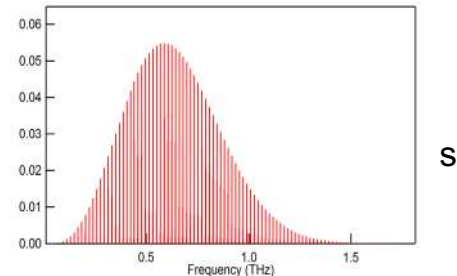
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(Pressure broadening linewidth = 23 MHz @H<sub>2</sub>O:10Pa&N<sub>2</sub>:320Pa)



## Sample Acetonitrile (CH<sub>3</sub>CN) gas



- ✓ Sy
- ✓ Int
- ✓ Inc
- ✓ Vo
- ✓ Br
- es



$B$ : rotational constant (= 9.194 GHz)  
 $D_{JK}$ : centrifugal distortion constant (= 17.67 MHz)  
 $J, K$ : rotational quantum numbers

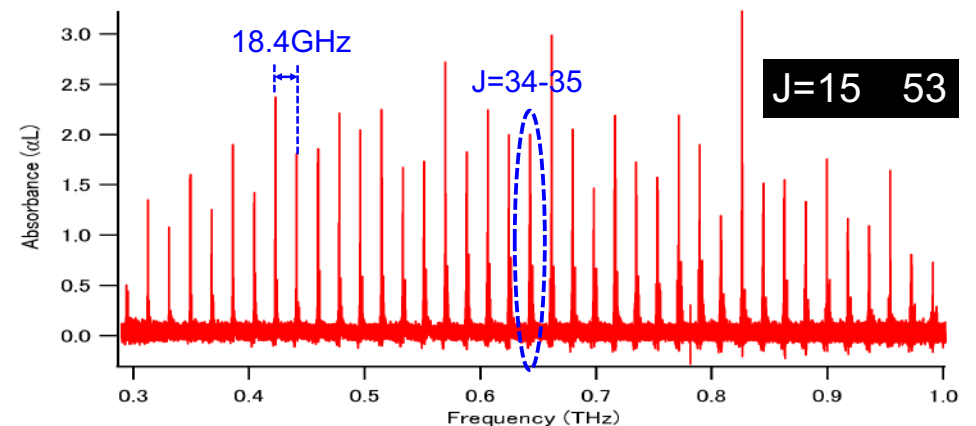
Rotational transitions

$$\nu = 2B(J+1) - 2D_{JK}K^2(J+1)$$

### Spectral signatures

- 1) A series of manifolds of rotational transitions regularly spaced by  $2B$
- 2) Hyperfine structure of rotational transitions into each manifold determined by  $D_{JK}$

Mode linewidth = sampling interval = 25 MHz Gas pressure=40Pa

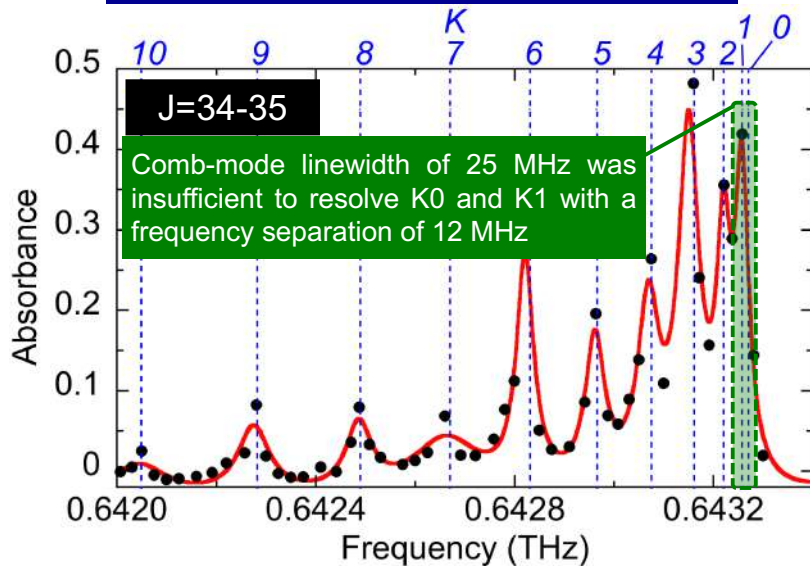


A series of rotational transition at interval of  $2B$  (=18.4GHz)

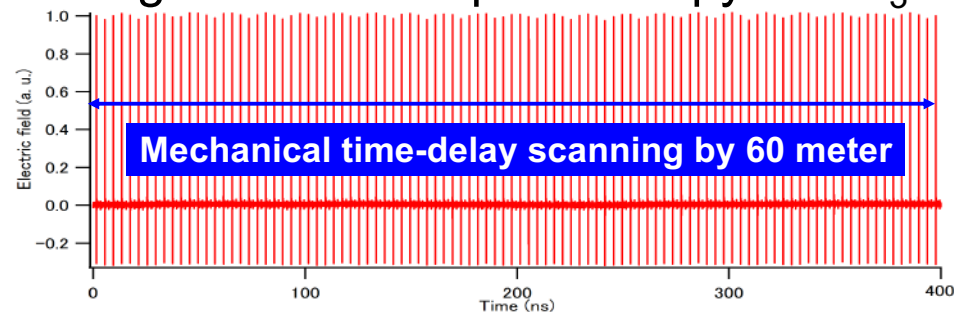


# High-resolution spectroscopy of CH<sub>3</sub>CN

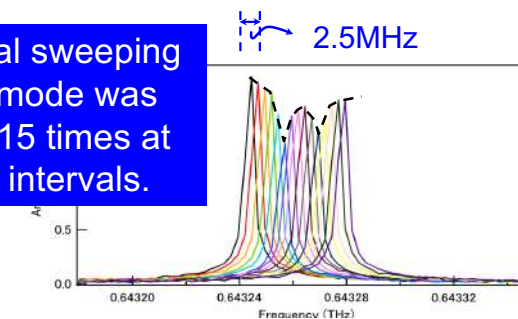
Mode linewidth = sampling interval = 25 MHz



# Ultrahigh-resolution spectroscopy of CH<sub>3</sub>CN

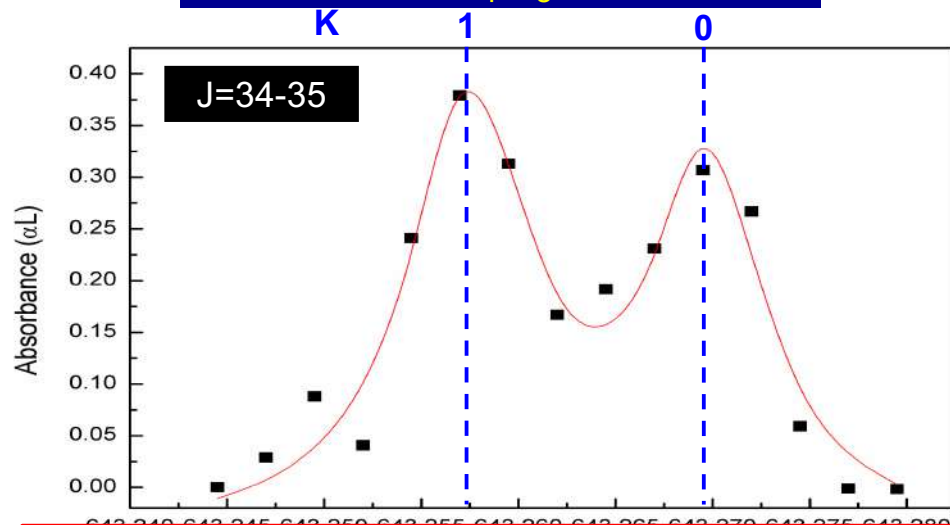


Incremental sweeping of comb mode was repeated 15 times at 2.5 MHz intervals.



# Ultrahigh-resolution spectroscopy of CH<sub>3</sub>CN

Mode linewidth = sampling interval = 2.5 MHz



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# Comparison of absorbance peak positions with NASA database in CH<sub>3</sub>CN

Line number (K)	NASA database (THz)	Experimental value (THz)	Discrepancy (MHz)
10	0.642049	0.642046	3
9	0.642280	0.642276	4
8	0.642487	0.642488	1
7	0.642670	0.642664	6
6	0.642829	0.642821	8
5	0.642963	0.642961	2
4	0.643074	0.643068	6
3	0.643159	0.643150	9
2	0.643220	0.643216	4
1	0.643257	0.643257	0.62
0	0.643269	0.643269	0.26

Comb mode linewidth = sampling interval = 25MHz

Comb mode linewidth = sampling interval = 2.5MHz

Corresponding to spectral accuracy of 10<sup>-7</sup>

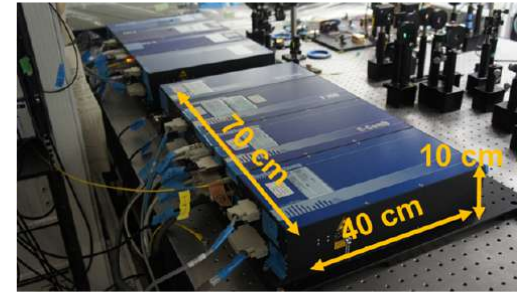
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# Limiting factors for practical application

## Dual stabilized fiber lasers

## Laser stabilization system



- (1) Use of dual fs lasers  
→ Single fs laser
- (2) Precise stabilization of  $\Delta f_{rep}$   
→ Free-running fs laser

How **dual** pulse lights with different  $f_{rep}$  can be generated by a **single** fs laser?

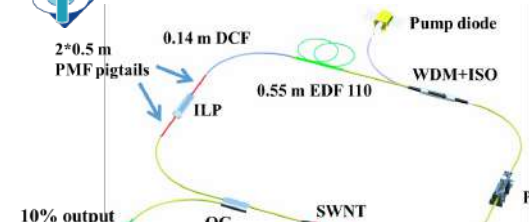
**ANSWER**

## Dual-wavelength mode-locked Er-doped fiber laser

- ✓ Simultaneous and independent mode-locking of two different-wavelength lights in the same cavity
- ✓ Material dispersion in a fiber cavity makes  $f_{rep}$  a slightly different between two wavelength lights
- ✓ Share of the same cavity fluctuates  $f_{rep1}$  and  $f_{rep2}$  in the common-mode manner, leading to the stable  $\Delta f_{rep}$

Ref) Hu, CLEO-PR2015, 26A3\_7; Sci. Rep. 7, 42082 (2017).

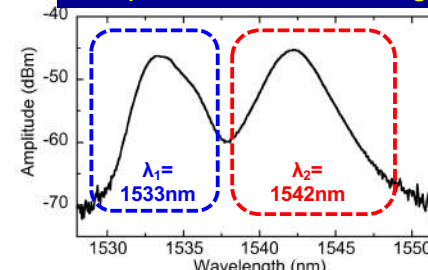
# Dual- $\lambda$ mode-locked Er-fiber laser



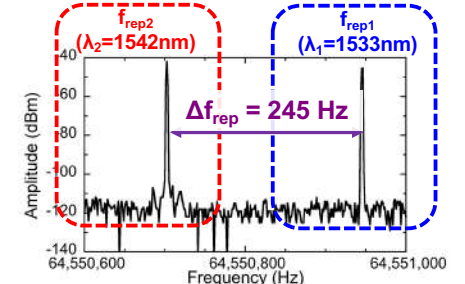
- Mode-locking by SWNT
- Dual- $\lambda$  ML oscillation by Lyot filter and gain modulation

## Slightly detuned $f_{rep1}$ and $f_{rep2}$

## Independent mode-locking

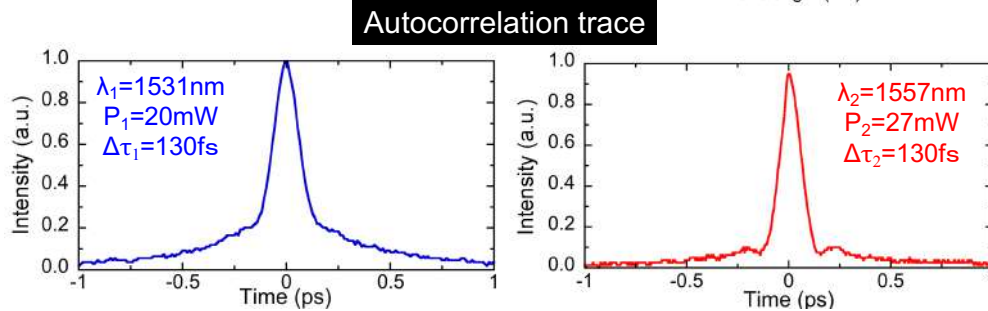
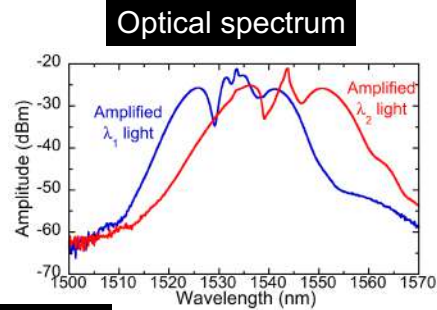
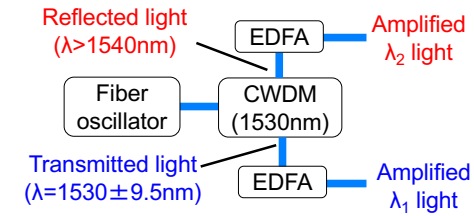


Optical spectrum



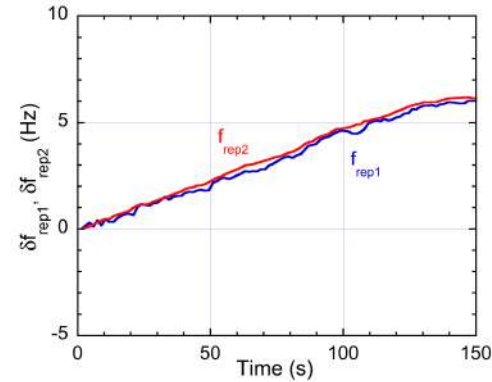
RF spectrum

# Separated and amplified dual- $\lambda$ light

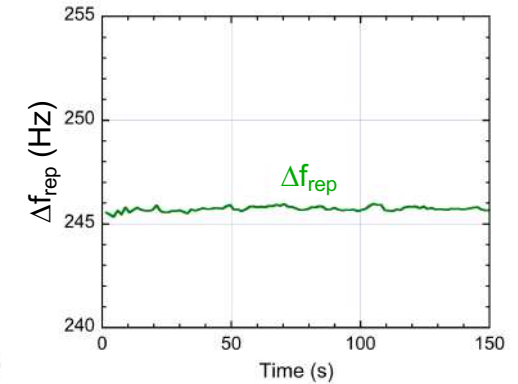


# Characteristics of $f_{\text{rep}1}$ , $f_{\text{rep}2}$ , $\Delta f_{\text{rep}}$

## Temporal change of $f_{\text{rep}1}$ and $f_{\text{rep}2}$



## Temporal change of $\Delta f_{\text{rep}}$



**Stable  $\Delta f_{\text{rep}}$  without the need for active stabilization**

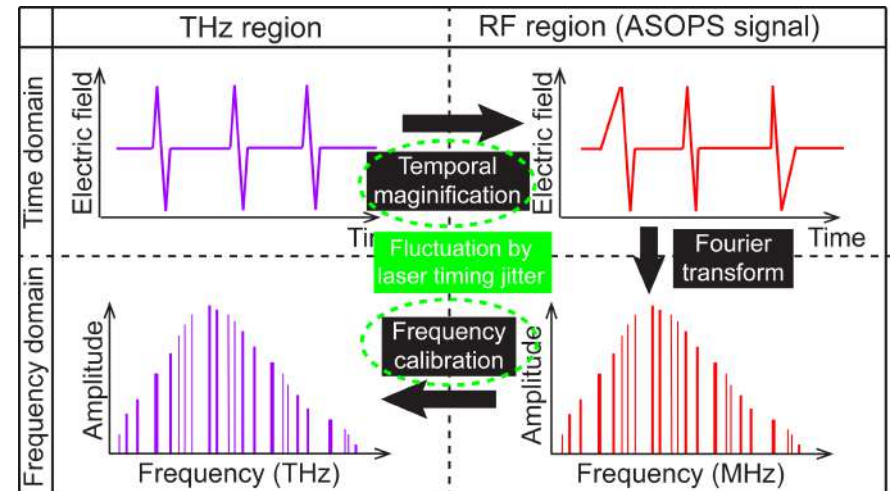
# Precisely stabilized, dual fs lasers

have been used in previous researches of THz-DCS

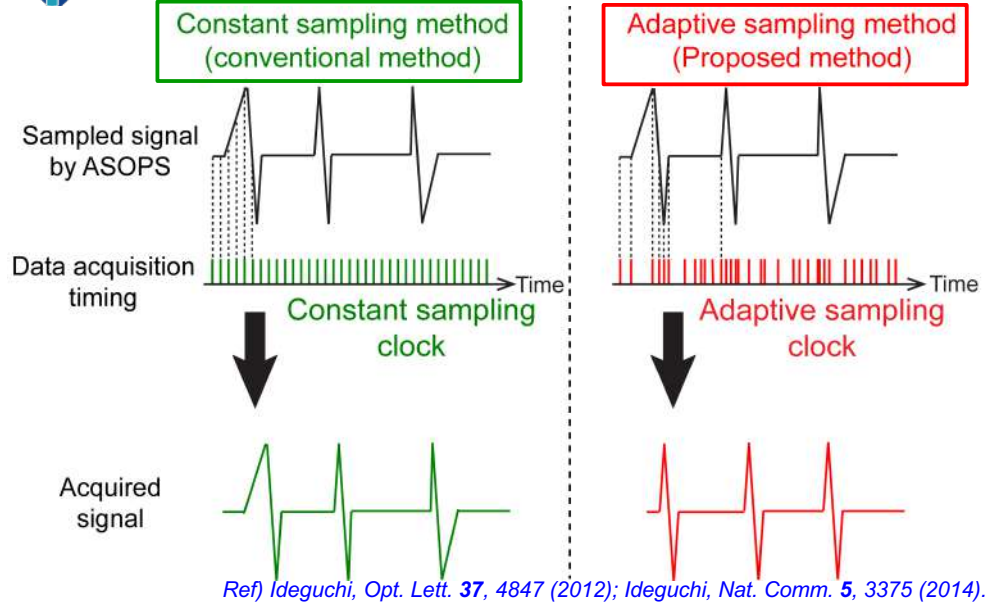
Use of **free-running**, dual- $\lambda$  mode-locked Er-fiber laser expands application fields of THz-DCS

**However, influence of timing jitter between free-running dual lasers has to be considered!**

# Influence of timing jitter in THz-DCS

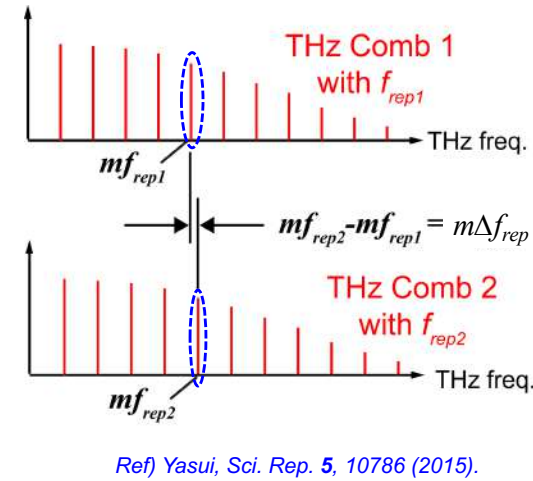


# Adaptive sampling method



# Adaptive sampling clock for $f_{rep}$

Beat signal between dual THz combs, which is a harmonic component of  $\Delta f_{rep} (= m\Delta f_{rep} = mf_{rep2} - mf_{rep1}) !!$

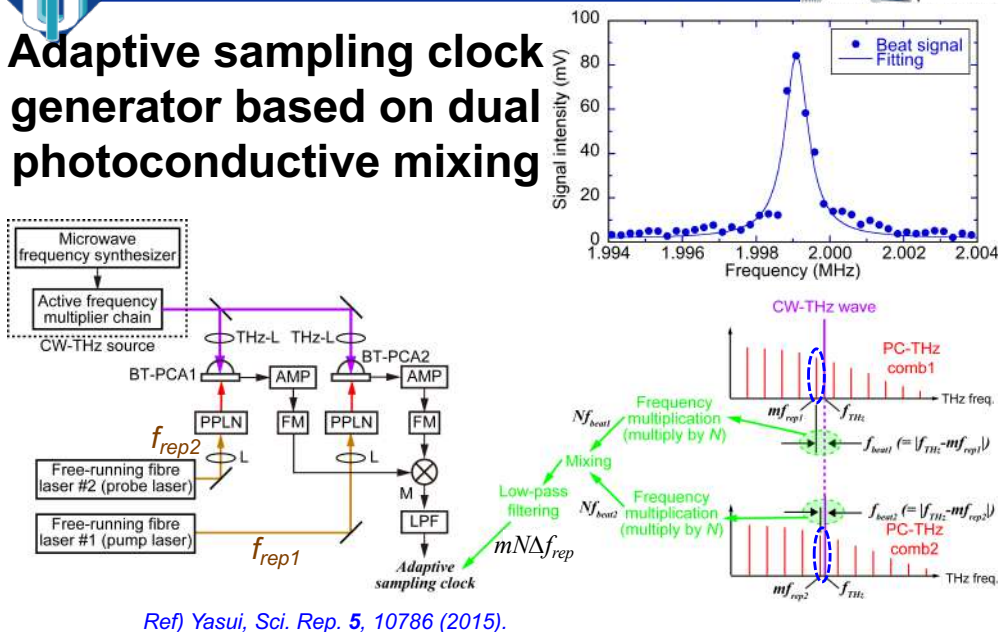


Comb mode is too dense and too weak!

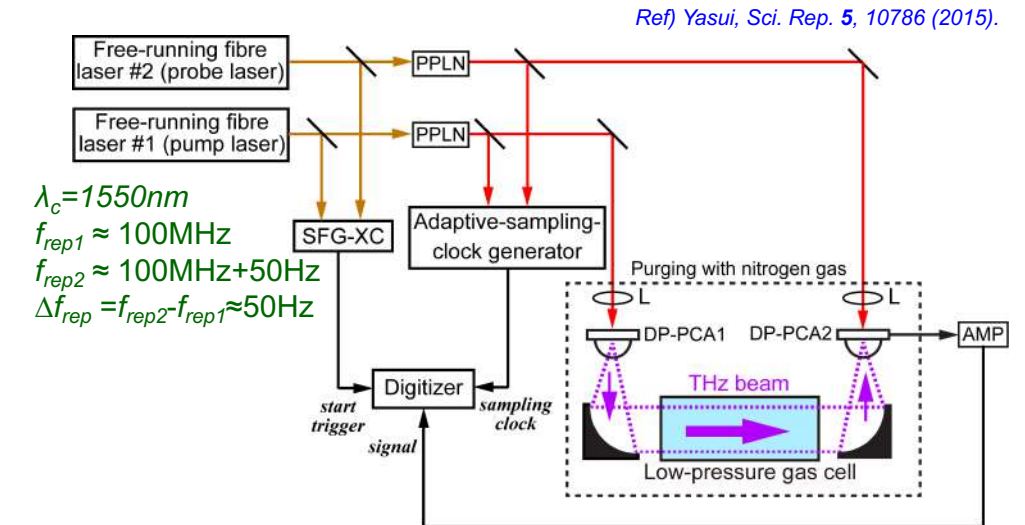
Difficult to extract a single mode from THz comb directly!

Photoconductive mixing between CW-THz radiation and PC-THz comb

# Adaptive sampling clock generator based on dual photoconductive mixing



# Experimental setup for THz-DCS

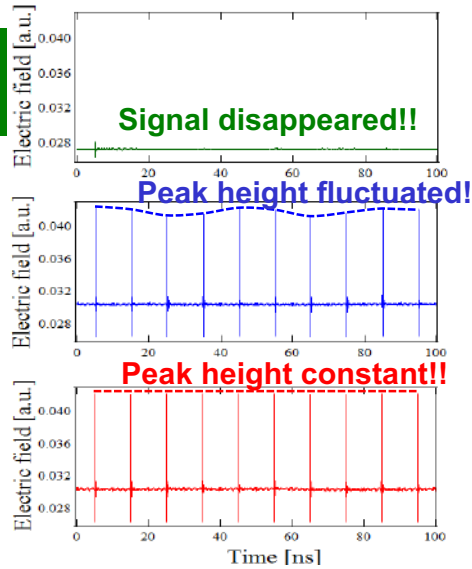


# Integrated temporal waveform of THz pulse

(time window = 100 ns, sampling interval = 100 fs, integration number = 10,000)

Ref) Yasui, *Sci. Rep.* 5, 10786 (2015).

Constant sampling  
with free-running lasers



Constant sampling  
with stabilized lasers

RMS timing jitter (0.1 Hz-500 kHz)  
< 150 fs

Freq. ref.: Rb atomic clock (stability  $10^{-11}$ )

Adaptive sampling  
with free-running lasers

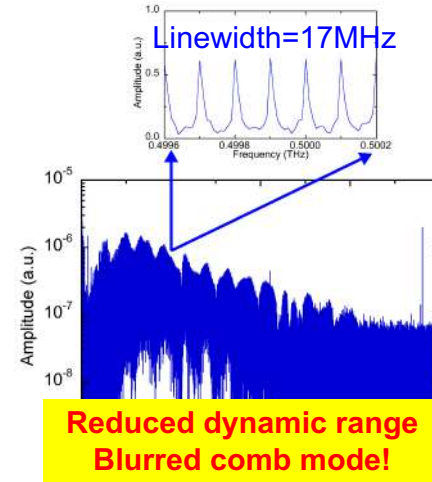


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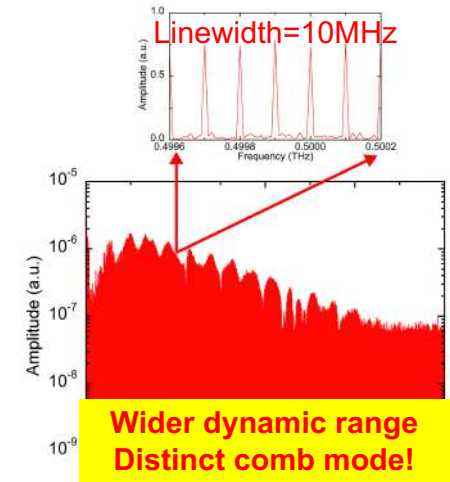


# Mode-resolved THz comb spectrum

Constant sampling  
with stabilized lasers



Adaptive sampling  
with free-running lasers

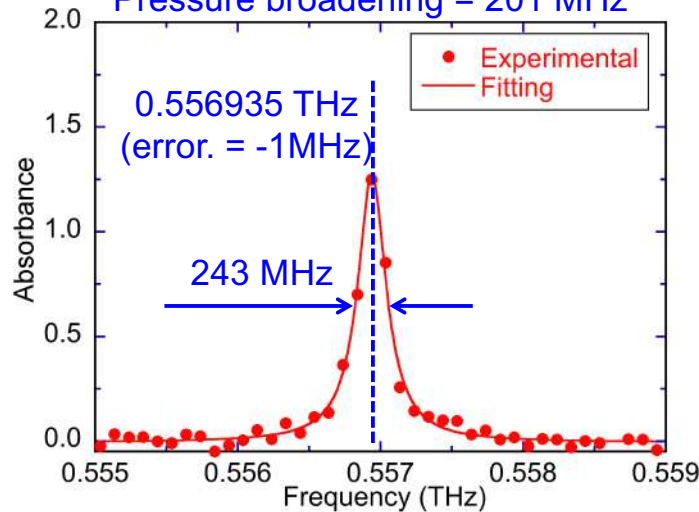


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# Low-pressure water vapor (145Pa)

Asymmetric top molecule,  $1_{10} \leftarrow 1_{01}$  @ 0.5569365 THz,  
Pressure broadening = 201 MHz

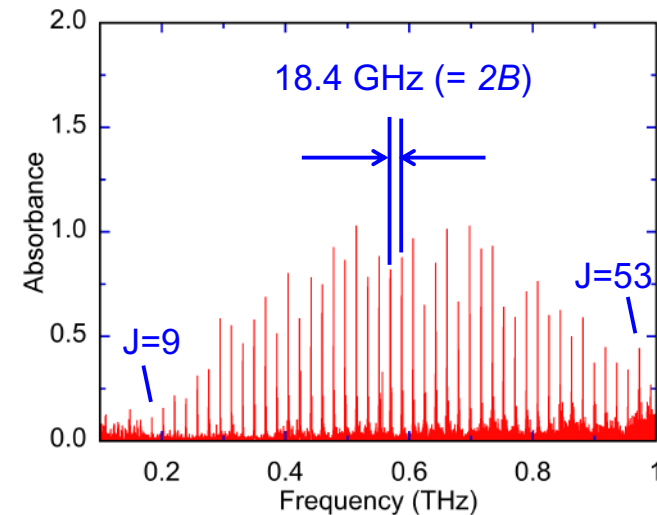


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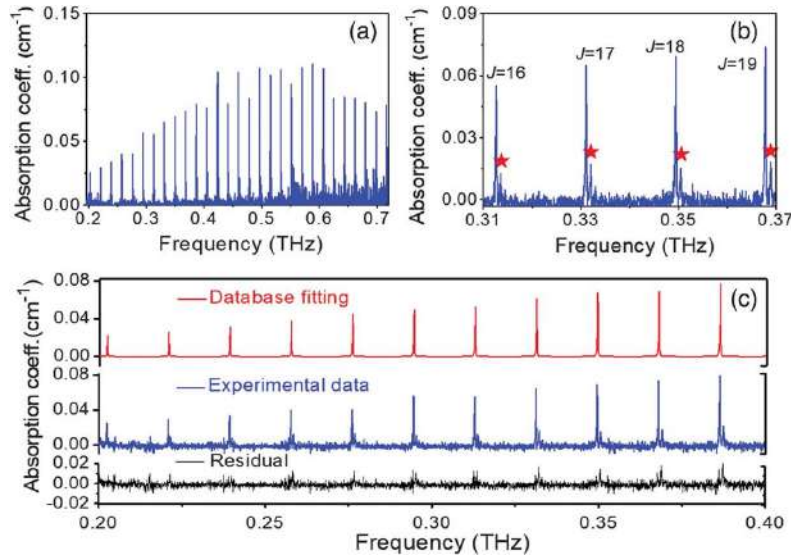


# Acetonitrile gas at low pressure (1kPa)

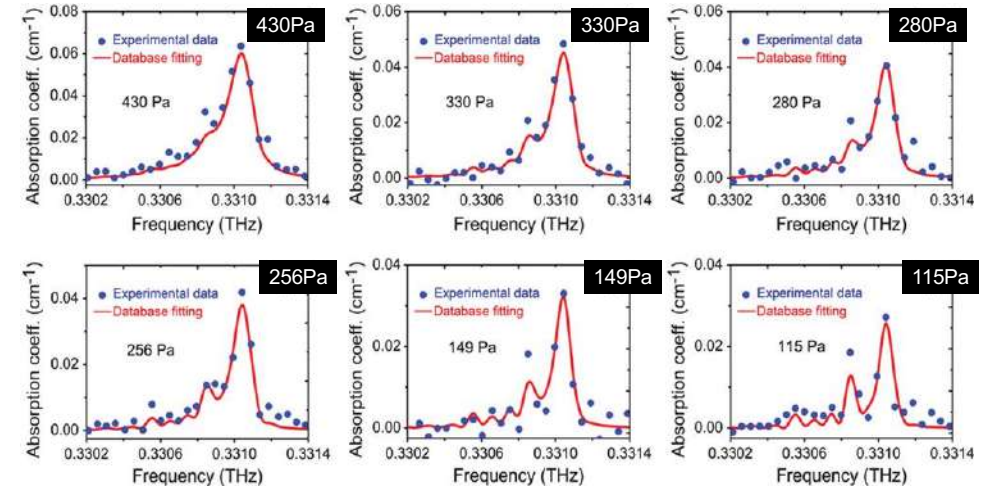
Symmetric molecule, rotational constant  $B = 9.2$  GHz



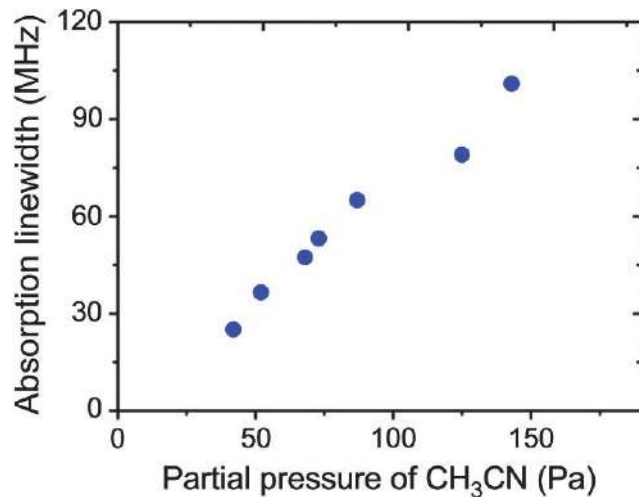
## Comb-mode-resolved THz spectroscopy of a mixture gas sample of CH<sub>3</sub>CN and air with a total pressure of 360 Pa



## Mode-resolved absorption characterization of CH<sub>3</sub>CN around 0.331 THz



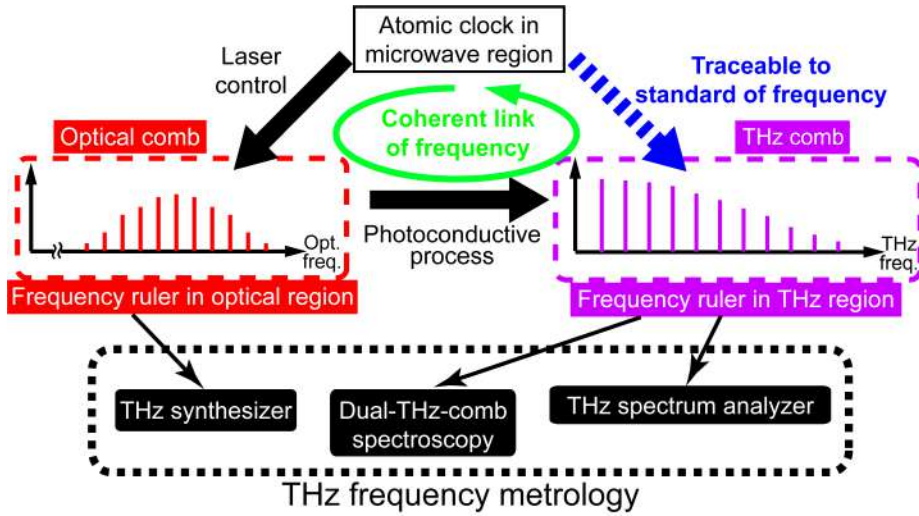
## Pressure broadening characteristic of CH<sub>3</sub>CN/air gas



## Outline

1. Introduction
2. Dual THz comb spectroscopy (THz-DCS)
3. Gapless THz-DCS
4. Adaptive sampling THz-DCS using a single, free-running fiber laser
5. Summary

# THz frequency metrology based on frequency comb



# Coherent link of frequency

